



Time: 2 Hours

[Total Marks: 40]

PART-A

- Instructions:**
1. Answer the following questions
 2. Each question carries **ONE** mark

8 X 1 = 8

1. Find the particular integral of $(D^2 + 1)y = 17$
2. Find the value of a_0 for $f(x) = (\pi - x)$ in the interval $(0, \pi)$.
3. Find the Laplace Transform of $t^4 + e^{2t}$
4. Write the nature of the roots of auxiliary equation of Diifferential Equation.
 $(D^2 - 2D)y = 0$
5. Write the second shifting theorem Laplace transform.
6. Find $L\{e^{3t} - e^t - 3t\}$
7. Find $L^{-1}\left\{\frac{1}{s^2 + 5}\right\}$
8. Find $L^{-1}\left\{\frac{1}{(s-2)^3}\right\}$

PART-B

- Instructions:**
1. Answer the following questions
 2. Each question carries **THREE** marks

4 X 3 = 12

- 9(a). Solve $(D^2 + 4)y = 0$
----- OR -----
- 9(b). Find $L\left(\frac{\sin t}{t}\right)$
- 10(a). Find the value of b_n for the function $f(x) = x$ which is expanded as sine series $(0, \pi)$
----- OR -----
- 10(b). Find $L^{-1}\left\{\frac{3s - 12}{s^2 + 8}\right\}$

15 11(a). Find $\mathcal{L}\left((1+t^2)^2\right)$ 005

----- OR -----

11(b). Find $\mathcal{L}\left(e^{-2t}(3\sin 4t - 4\cos 4t)\right)$

12(a). Find $\mathcal{L}^{-1}\left\{\frac{s^2 - 3s + 4}{s^4}\right\}$

----- OR -----

12(b). Find $\mathcal{L}^{-1}\left\{\frac{e^{-3s}}{(s+4)^2}\right\}$ using second shifting theorem

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PART-C

Instructions:

1. Answer the following questions
2. Each question carries **FIVE** marks

4 X 5 = 20

13(a). Solve $(D^3 - 9D^2 + 23D - 15)Y = 0$

----- OR -----

13(b). Find $\mathcal{L}\{t^2 \cos 2t\}$

14(a). Find the Fourier series expansion of $f(x) = x, 0 \leq x \leq 2\pi$.

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----- OR -----

14(b). Find $\mathcal{L}^{-1}\left[\frac{3s - 2}{s^2 - 2s + 5}\right]$

15(a). Evaluate $\int_0^{\infty} te^{-2t} \sin t dt$

----- OR -----

15(b). Evaluate $\int_0^{\infty} te^{-2t} \cos t dt$ using Laplace transform

05 16(a). Using Convolution Theorem, find $\mathcal{L}^{-1}\left\{\frac{s}{(s^2+1)(s^2+4)}\right\}$

----- OR -----

16(b). Find the Inverse laplace Transform of $\frac{s^2}{(s+1)(s+2)(s+3)}$